

PHYS 393  
Low Temperature Physics  
Set 6:

Superfluid  $\text{He}^3$

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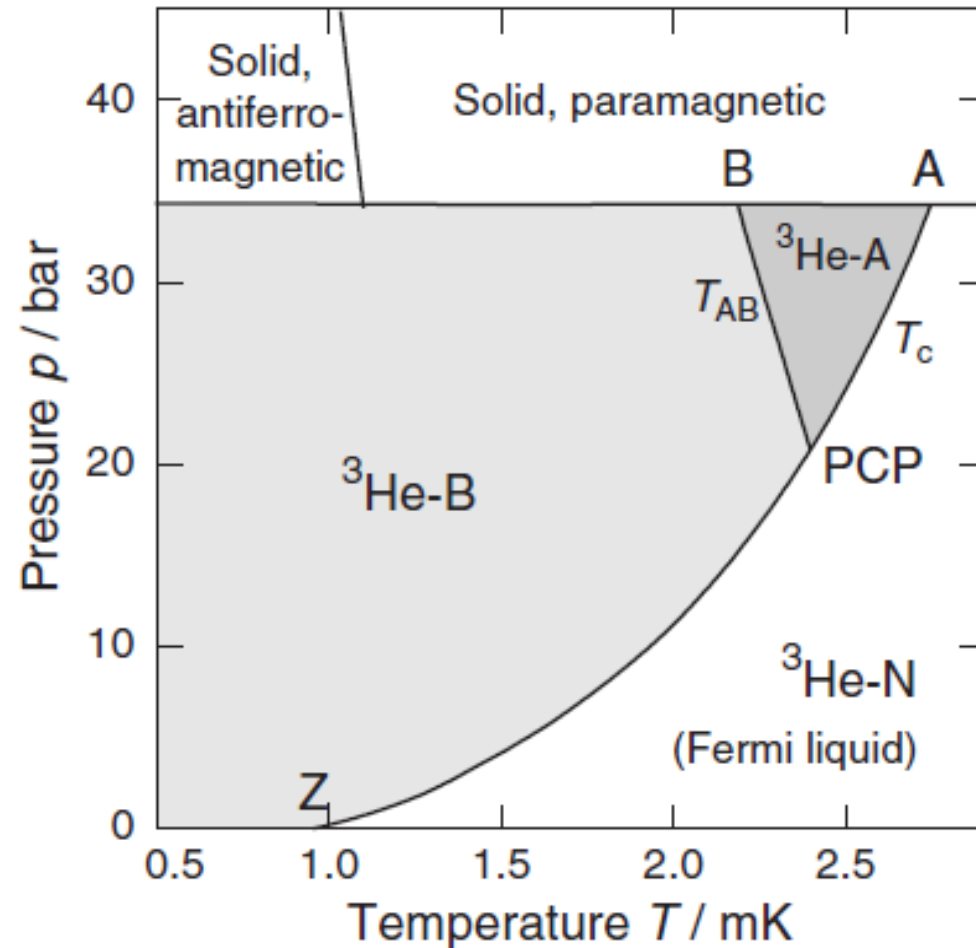
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# Superfluidity in $\text{He}^3$

- BEC condensation not possible in  $\text{He}^3$  (fermions)
- BCS theory (1957) provided a mechanism
- Not exact analogy to superconductivity
- Many experimental efforts; problematic  $T_c$  theoretical estimates
- Discovery in 1971 around 2mK (Osheroff, Richardson, Lee)
- Initially thought it was a new solid phase
- Superfluidity soon proven by NMR experiments

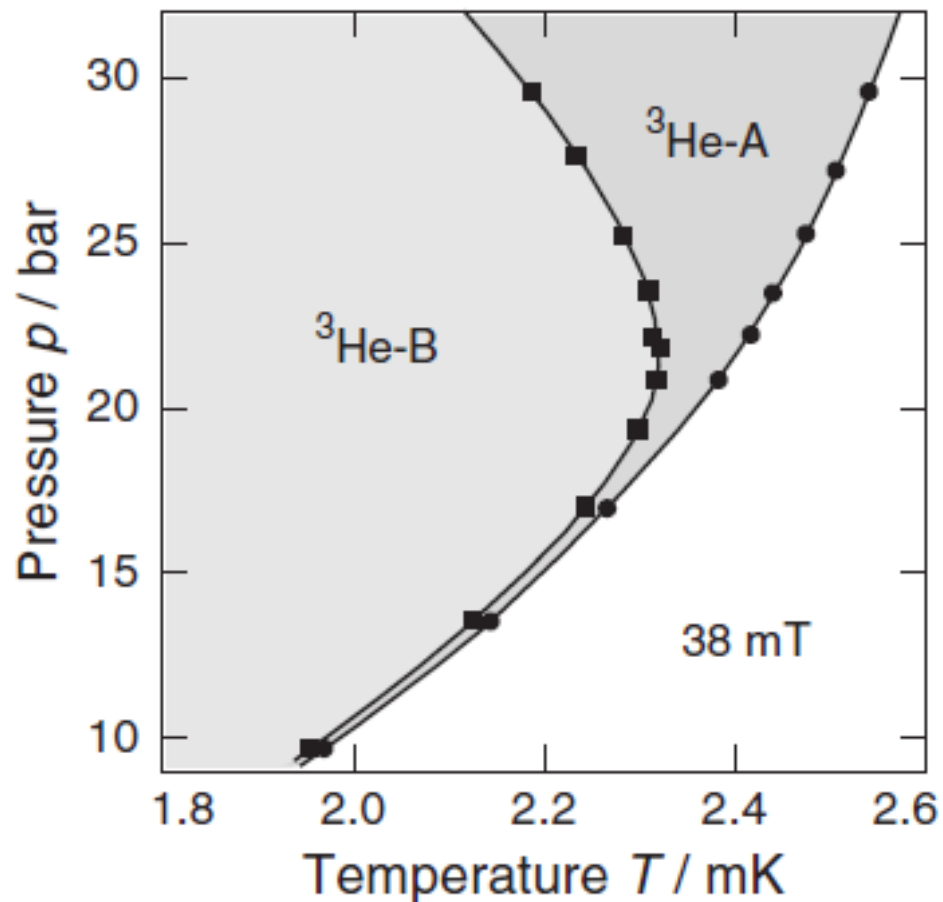
# He<sup>3</sup> pressure-temperature phase diagram

- Behaviour below 3mK in absence of magnetic fields
- Two superfluid phases (shaded): A and B
- PCP: polycritical point (coexistence of three liquid phases)



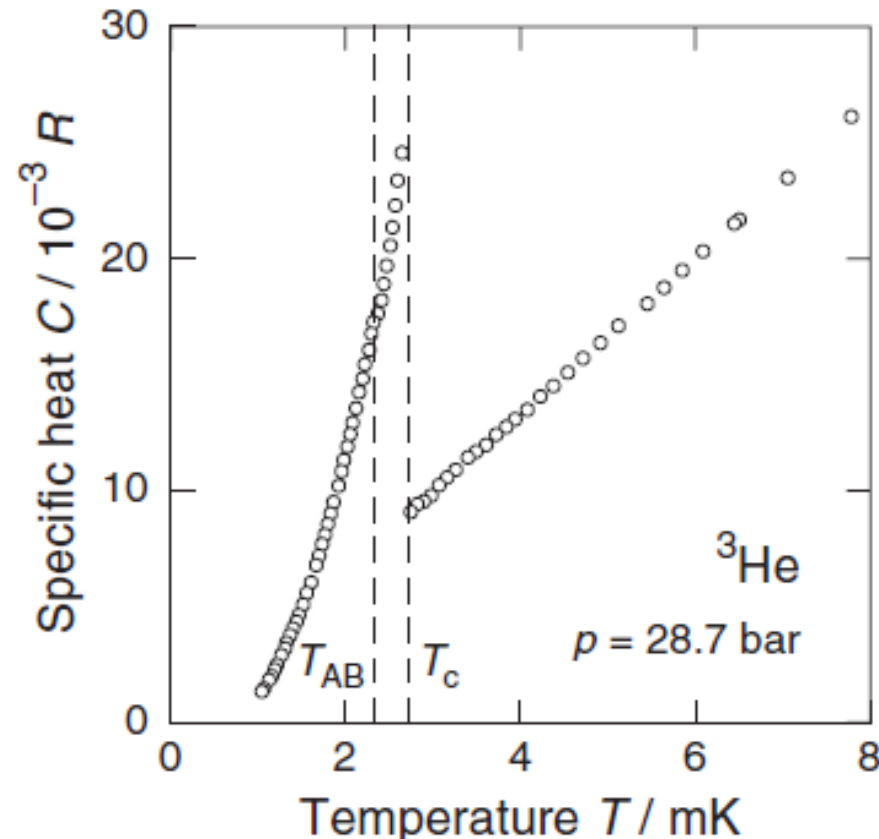
# He<sup>3</sup> phase diagram in magnetic field

- Different behaviour in presence of magnetic field (graph for 38mT)
- PCP disappears
- Phase A widens
- Above 0.65T Phase B disappears



# Phase transition

- Specific heat (graph): phase transition at  $T_C$
- Small effect at  $T_{AB}$  (transition from phase A to phase B)
- Viscosity (damping of vibrating wire experiment): drop of damping force by 5 orders of magnitude between 1mK and 0.14mK
- Behaviour consistent with two-fluid model
- Proportion of superfluid increases as temperature decreases



## Two-fluid model in $\text{He}^3$

- Superfluid seen as  $\text{He}^3$  pairs in ground state
- Normal fluid seen as single  $\text{He}^3$  atoms in excited states
- All superfluid as  $T \rightarrow 0$
- Strength of pairing interaction determines critical temperature  $T_c$
- Weak interaction:  $T_c \sim 2\text{mK}$

# Pairing mechanism

- Not phonons but magnetic interaction
  - First atom polarizes surrounding atoms
  - Second atom interacts with "polarization trail"
- Complex details
- In superconductors pairs have  $S=0$ ,  $L=0$
- $\text{He}^3$  atom pairs have  $S=1$  (shown experimentally)
- Pauli principle requires total wavefunction to be antisymmetric WRT particle exchange
- Hence total orbital angular momentum must be odd - in practice  $L=1$
- Superfluid  $\text{He}^3$ : pairs with  $S=1$ ,  $L=1$ 
  - Spin triplet or odd parity pairing

# Spin-triplet pairing

Spin of pair determined by  $|S, S_z\rangle$

Three different spin states:

$$S_z = +1 \quad |1, +1\rangle = |\uparrow\uparrow\rangle,$$

$$S_z = 0 \quad |1, 0\rangle = \frac{1}{\sqrt{2}} [|\uparrow\downarrow\rangle + |\downarrow\uparrow\rangle],$$

$$S_z = -1 \quad |1, -1\rangle = |\downarrow\downarrow\rangle$$

Phase A contains  $S_z=+1, S_z=-1$

Phase B contains  $S_z=+1, S_z=0, S_z=-1$

Phase A is more magnetic than Phase B, as all pairs have non-zero magnetic moment

For field  $B > 0.6\text{ T}$  phase B disappears

New phase A1 appears as thin slice between normal fluid and Phase A, thought to be pure  $S_z=+1$  or pure  $S_z=-1$



# Alignment

- $\text{He}^3$  superfluidity due to (weak) magnetic dipole-dipole interaction
- Pairs have perpendicular  $L$ ,  $S$  vectors (minimizes energy)

Phase A:

- $L$  vector perpendicular to container walls
- $L$  vector perpendicular to  $S$  vector
- Inside magnetic field  $S$  vector aligns parallel to  $B$  vector
- Competing requirements produce complex, anisotropic effects

Phase B more complex

# Conclusions on superfluid He3

- Atom-pair bosons
- Weak magnetic dipole-dipole interactions
- BEC condensate (pairs in ground state)
- Complex effects
- Strong effects from external magnetic and electric fields, container walls